

# ETSI TS 145 004 V4.1.0 (2001-04)

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*Technical Specification*

## Digital cellular telecommunications system (Phase 2+); Modulation (3GPP TS 45.004 version 4.1.0 Release 4)

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GLOBAL SYSTEM FOR  
MOBILE COMMUNICATIONS



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**Reference**

DTS/TSGG-0145004Uv4

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**Keywords**

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# Foreword

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## 0 Scope

The modulator receives the bits from the encryption unit, see GSM 05.01 [1], and produces an RF signal. The filtering of the Radio Frequency (RF) signal necessary to obtain the spectral purity is not defined, neither are the tolerances associated with the theoretical filter requirements specified. These are contained in GSM 05.05 [4].

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## 1a References

The following documents contain provisions which, through reference in this text, constitute provisions of the present document.

- References are either specific (identified by date of publication, edition number, version number, etc.) or non-specific.
- For a specific reference, subsequent revisions do not apply.
- For a non-specific reference, the latest version applies. In the case of a reference to a 3GPP document (including a GSM document), a non-specific reference implicitly refers to the latest version of that document *in the same Release as the present document*.

- [1] GSM 01.04: "Digital cellular telecommunication system (Phase 2+); Abbreviations and acronyms".
- [2] GSM 05.01: "Digital cellular telecommunication system (Phase 2+); Physical layer on the radio path General description".
- [3] GSM 05.02: "Digital cellular telecommunication system (Phase 2+); Multiplexing and multiple access on the radio path".
- [4] GSM 05.05: "Digital cellular telecommunication system (Phase 2+); Radio transmission and reception".

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## 1b Abbreviations

Abbreviations used in this specification are listed in GSM 01.04 [1]

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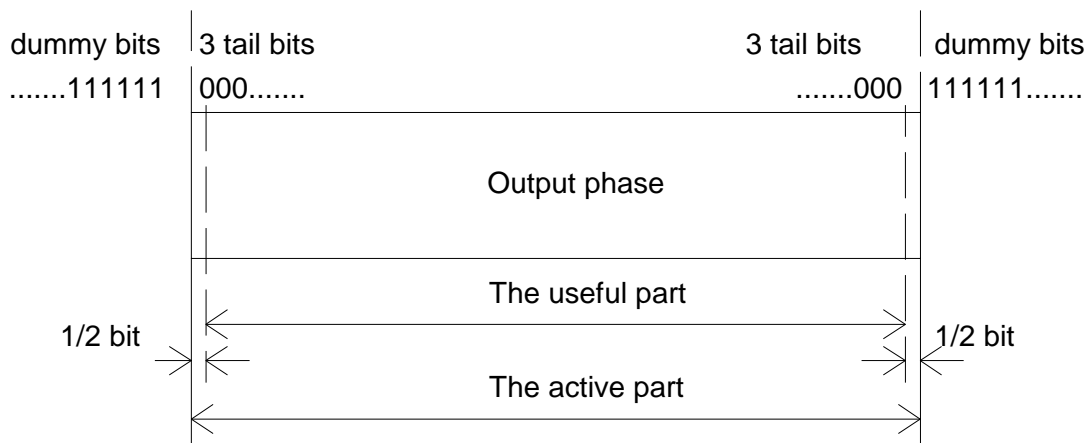
## 2 Modulation format for GMSK

### 2.1 Modulating symbol rate

The modulating symbol rate is  $1/T = 1\ 625/6$  ksymb/s (i.e. approximately 270.833 ksymb/s), which corresponds to  $1\ 625/6$  kbit/s (i.e. 270.833 kbit/s). T is the symbol period.

### 2.2 Start and stop of the burst

Before the first bit of the bursts as defined in GSM 05.02 [3] enters the modulator, the modulator has an internal state as if a modulating bit stream consisting of consecutive ones ( $d_i = 1$ ) had entered the differential encoder. Also after the last bit of the time slot, the modulator has an internal state as if a modulating bit stream consisting of consecutive ones ( $d_j = 1$ ) had continued to enter the differential encoder. These bits are called dummy bits and define the start and the stop of the active and the useful part of the burst as illustrated in figure 1. Nothing is specified about the actual phase of the modulator output signal outside the useful part of the burst.



**Figure 1: Relation between active part of burst, tail bits and dummy bits. For the normal burst the useful part lasts for 147 modulating bits**

### 2.3 Differential encoding

Each data value  $d_i = [0,1]$  is differentially encoded. The output of the differential encoder is:

$$\hat{d}_i = d_i \oplus d_{i-1} \quad (d_i \in \{0,1\})$$

where  $\oplus$  denotes modulo 2 addition.

The modulating data value  $\alpha_i$  input to the modulator is:

$$\alpha_i = 1 - 2\hat{d}_i \quad (\alpha_i \in \{-1,+1\})$$

### 2.4 Filtering

The modulating data values  $\alpha_i$  as represented by Dirac pulses excite a linear filter with impulse response defined by:

$$g(t) = h(t) * \text{rect}\left(\frac{t}{T}\right)$$

where the function  $\text{rect}(x)$  is defined by:

$$\text{rect}\left(\frac{t}{T}\right) = \frac{1}{T} \quad \text{for } |t| < \frac{T}{2}$$

$$\text{rect}\left(\frac{t}{T}\right) = 0 \quad \text{otherwise}$$

and  $*$  means convolution.  $h(t)$  is defined by:

$$h(t) = \frac{\exp\left(\frac{-t^2}{2\delta^2 T^2}\right)}{\sqrt{(2\pi) \cdot \delta T}}$$

where 
$$\delta = \frac{\sqrt{\ln(2)}}{2\pi BT} \quad \text{and } BT = 0.3$$

where B is the 3 dB bandwidth of the filter with impulse response  $h(t)$ . This theoretical filter is associated with tolerances defined in GSM 05.05 [4].

## 2.5 Output phase

The phase of the modulated signal is:

$$\varphi(t') = \sum_i \alpha_i \pi h \int_{-\infty}^{t'-iT} g(u) du$$

where the modulating index  $h$  is 1/2 (maximum phase change in radians is  $\pi/2$  per data interval).

The time reference  $t' = 0$  is the start of the active part of the burst as shown in figure 1. This is also the start of the bit period of bit number 0 (the first tail bit) as defined in GSM 05.02 [2].

## 2.6 Modulation

The modulated RF carrier, except for start and stop of the TDMA burst may therefore be expressed as:

$$x(t') = \sqrt{\frac{2E_c}{T}} \cdot \cos(2\pi f_0 t' + \varphi(t') + \varphi_0)$$

where  $E_c$  is the energy per modulating bit,  $f_0$  is the centre frequency and  $\varphi_0$  is a random phase and is constant during one burst.

# 3 Modulation format for 8PSK

## 3.1 Modulating symbol rate

The modulating symbol rate is  $1/T = 1 \cdot 625/6$  ksymb/s (i.e. approximately 270.833 ksymb/s), which corresponds to  $3 \cdot 1 \cdot 625/6$  kbit/s (i.e. 812.5 kbit/s). T is the symbol period.

## 3.2 Symbol mapping

The modulating bits are Gray mapped in groups of three to 8PSK symbols by the rule

$$s_i = e^{j2\pi l/8}$$

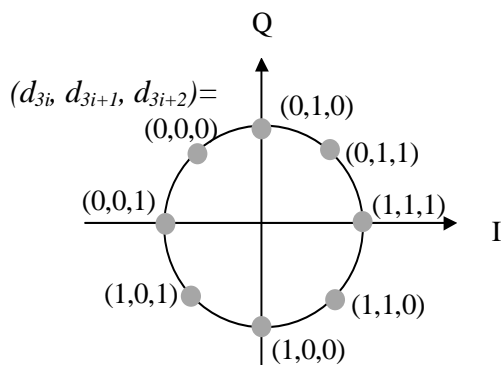
where  $l$  is given by table 1.



**Table 1: Mapping between modulating bits and the 8PSK symbol parameter  $l$ .**

Modulating bits $d_{3i}, d_{3i+1}, d_{3i+2}$	Symbol parameter $l$
(1,1,1)	0
(0,1,1)	1
(0,1,0)	2
(0,0,0)	3
(0,0,1)	4
(1,0,1)	5
(1,0,0)	6
(1,1,0)	7

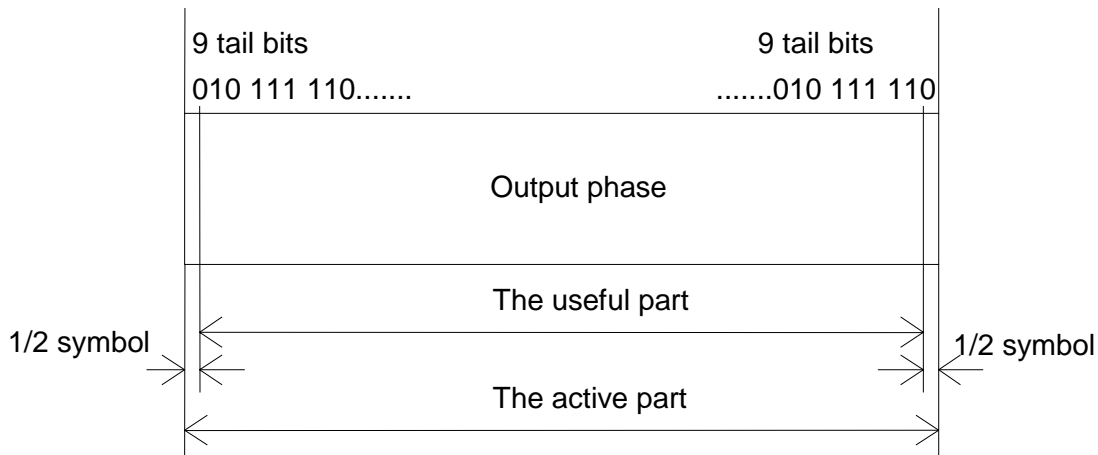
This is illustrated in figure 2.



**Figure 2: Symbol mapping of modulating bits into 8PSK symbols.**

### 3.3 Start and stop of the burst

Before the first bit of the bursts as defined in GSM 05.02 [3] enters the modulator, the state of the modulator is undefined. Also after the last bit of the burst, the state of the modulator is undefined. The tail bits (see GSM 05.02) define the start and the stop of the active and the useful part of the burst as illustrated in figure 3. Nothing is specified about the actual phase of the modulator output signal outside the useful part of the burst.



**Figure 3: Relation between active part of burst and tail bits. For the normal burst the useful part lasts for 147 modulating symbols**

### 3.4 Symbol rotation

The 8PSK symbols are continuously rotated with  $3\pi/8$  radians per symbol before pulse shaping. The rotated symbols are defined as

$$\hat{s}_i = s_i \cdot e^{j3\pi/8}$$

### 3.5 Pulse shaping

The modulating 8PSK symbols  $\hat{s}_i$  as represented by Dirac pulses excite a linear pulse shaping filter. This filter is a linearised GMSK pulse, i.e. the main component in a Laurant decomposition of the GMSK modulation. The impulse response is defined by:

$$c_0(t) = \begin{cases} \prod_{i=0}^3 S(t+iT), & \text{for } 0 \leq t \leq 5T \\ 0, & \text{else} \end{cases}$$

where

$$S(t) = \begin{cases} \sin(\pi \int_0^t g(t') dt'), & \text{for } 0 \leq t \leq 4T \\ \sin(\frac{\pi}{2} - \pi \int_0^{t-4T} g(t') dt'), & \text{for } 4T < t \leq 8T \\ 0, & \text{else} \end{cases}$$

$$g(t) = \frac{1}{2T} \left( Q\left(2\pi \cdot 0.3 \frac{t-5T/2}{T\sqrt{\log_e(2)}}\right) - Q\left(2\pi \cdot 0.3 \frac{t-3T/2}{T\sqrt{\log_e(2)}}\right) \right)$$

and

$$Q(t) = \frac{1}{\sqrt{2\pi}} \int_t^{\infty} e^{-\frac{\tau^2}{2}} d\tau.$$

The base band signal is

$$y(t') = \sum_i \hat{s}_i \cdot c_0(t'-iT + \frac{5}{2}T)$$

The time reference  $t' = 0$  is the start of the active part of the burst as shown in figure 3. This is also the start of the bit period of bit number 0 (the first tail bit) as defined in GSM 05.02 [2].

### 3.6 Modulation

The modulated RF carrier during the useful part of the burst is therefore:

$$x(t') = \sqrt{\frac{2E_s}{T}} \operatorname{Re} \left[ y(t') \cdot e^{j(2\pi f_0 t' + \varphi_0)} \right]$$

where  $E_s$  is the energy per modulating symbol,  $f_0$  is the centre frequency and  $\varphi_0$  is a random phase and is constant during one burst.

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## Annex A (informative): Change control history

SMG	SPEC	VERS	NEW_VE	PHA	SUBJECT
S27	05.04	5.0.1	6.0.0	R97	conversion to Release 97 EN
S28	05.04	6.0.0	8.0.0	R99	Introduction of 8PSK for EDGE
S30b	05.04	8.0.0	8.1.0	R99	Correction of mistake for range alpha-sub-i in Clause 2.3
		8.1.0	8.1.1		Figure 3 replaced (as it was corrupted)
G03	05.04	8.1.1	8.2.0	R99	Correction of symbol period notation
G04	45.004	8.2.0	4.0.0	Rel-4	New version for Release 4

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# History

<b>Document history</b>		
V4.1.0	April 2001	Publication